# Opposites Attract? Opportunities and Challenges for Integrating Large-N QCA and Econometric Analysis

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#### Abstract

Contrasting insights that can be gained from large-N QCA and econometric analysis, we outline two novel ways to integrate both modes of inquiry. The first introduces QCA solutions into a regression model, while the second draws on recent work in lattice theory to integrate a QCA approach with a regression framework. These approaches allow researchers to test QCA solutions for robustness, address concerns regarding possible omitted variables, establish effect sizes, and test whether causal conditions are complements or substitutes, suggesting that an important way forward for set-theoretic analysis lies in an increased dialogue that explores complementarities with existing econometric approaches.

## Introduction

In its original statement by Charles Ragin (1987), Qualitative Comparative Analysis (QCA) was conceived as a methodology for small-*N*, comparative work in the case-oriented tradition; a conception that still resonates with much of the current work using QCA (Rihoux and Ragin 2009). However, researchers have also applied QCA to examine large-*N* phenomena (e.g., Fiss 2011; Greckhamer, Misangyi, Elms, and Lacey 2008; Ragin and Fiss 2008; Vis 2012).<sup>1</sup> These large-*N* applications have prompted Greckhamer, Misangyi, and Fiss (forthcoming) to suggest that currently there are in fact "two QCAs" that differ in their focus on small- and large-*N* phenomena as well as in some of their assumptions, objectives, and analyses processes.

Several issues are raised by applying QCA to a larger number of cases. In particular, researchers applying this approach find themselves largely on the same research terrain as traditional large-*N* researchers using econometric tools usually based on the standard linear model. We believe that this has proven to be both an opportunity and a challenge. On the positive side, the application of QCA to large-*N* situations offers a considerable opportunity for both new empirical insights and new theory building. For instance, prior works that focus on hypothesis testing in particular have tended to develop theories based on correlational statements. As Ragin (2000, 2008) has argued, such thinking does not necessarily correspond to the

nature of causal relations present in social research. Accordingly, the introduction of QCA to a whole new series of phenomena carries a significant upside. However, this upside does not come without challenges. Chief among these is that in large-NQCA, it is difficult to maintain the kind of intimate familiarity with the cases that small-N QCA is usually based on. As a result, measurement errors in coding of cases are more likely. Contradictory observations in large-NQCA might then at times be accepted as measurement error, whereas in small-NQCA, they will frequently trigger a re-examination of the cases selected and whether all relevant causal conditions have been included. Due to this, establishing the robustness of QCA results is a more important concern in large-N applications than it is in small-N ones. In this article, we argue that there are two aspects in particular that need to be addressed for QCA to achieve its full potential as a method covering both small-N and large-N situations.

The first issue relates to distinguishing the unique contribution of QCA relative to existing econometric tools when both could be used in large-*N* situations. To help realize QCA's potential as a tool for large-*N* analysis, we briefly contrast large-*N* QCA with standard econometric approaches. This discussion is intended to lay the

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groundwork for the second issue, which focuses on potential synergies and ways to integrate the insights from QCA with other econometric tools. Specifically, we suggest that integrating QCA findings into a regression framework or a lattice-theoretic analysis that draws on recent work in lattice theory (Milgrom and Roberts 1990, 1995; Mohnen and Röller 2005) to mimic a QCA approach within a regression framework potentially allows for added insights regarding result robustness, effect sizes, complementarity and substitutability relationships between causal conditions, and the addition of causal conditions that otherwise would make a QCA too unwieldy. We conclude by suggesting that one way forward for set-theoretic analysis lies in an increased dialogue with existing econometric approaches.

## Contrasting Approaches: Large-N QCA versus Correlation-Based Approaches

There is no question that QCA and correlation-based approaches such as linear regression are rather different beasts. As Ragin has argued, QCA should first and foremost be seen as a research strategy that emphasizes the dialogue of ideas and evidence, not merely a technique of analyzing data. But differences do not end there "settheoretic relations concern explicit connections, while correlations address tendential connections; set-theoretic relations are asymmetrical, while correlations are sym*metrical*; set-theoretic relations are well suited for questions about necessity and sufficiency, while correlations are not; and so on" (Ragin 2005, 37; emphasis in original, see also Achen 2005 and Seawright 2005 for alternative views). Along similar lines, Vis (2012) argues that while regression analysis strives to explain the average effects of certain variables (causes), QCA seeks to identify the causes of particular outcomes (effects).

The contrasts between both approaches thus stand in fairly clear relief; however, there are also considerable similarities. As Greckhamer et al. (forthcoming) argue, large-N QCA is in fact well suited to hypothesis testing and deductive reasoning and by its very nature maintains a distance between the researcher and the cases, thus making large-N QCA applications in fact similar to conventional econometric approaches even as such QCA applications retain their configurational nature. Vis (2012), likewise, proposes that fuzzy-set QCA (fsQCA) moves toward identifying the effects of (multiple) causes rather than the causes of effects as the number of cases under study increases. To clarify this relationship, we contrast large-NQCA with standard econometric correlation-based approaches regarding their estimation procedures and their measures of model fit, with a focus on beginning a deeper engagement between these two approaches that are based on rather different epistemological and methodological assumptions.

#### Contrasting Estimation Procedures

QCA is a means of analyzing multiple cases to identify "recipes" of causal conditions associated with case membership in an outcome set (Ragin 2008). This approach allows for equifinality (different configurations leading to the same outcome), asymmetric causality (absence of causal conditions associated with an outcome not leading to absence of the outcome), and for differentiating between causally core and causally peripheral conditions (causally core conditions are part of both parsimonious and intermediate solutions, whereas causally peripheral conditions are part of the intermediate solution but are eliminated in the parsimonious one) (Fiss 2011; Ragin 2000, 2008). In contrast, most basic econometric models are premised on what Ragin has termed "net effects thinking," that is they estimate the impact of individual explanatory variables on a dependent variable, holding everything else constant. Such models implicitly assume unifinality, as the maximum value of the dependent variable is achieved by maximizing all explanatory variables that have positive coefficients, and symmetric causality, as the effect of a reduction in an explanatory variable on the outcome is equal and opposite to the effect of an increase of the same magnitude. Furthermore, many of these issues also apply to more advanced econometric approaches such as hierarchical linear models that aim to capture interactions across levels of analysis (e.g., Lacey and Fiss 2009).

Although approaches such as interaction effects, cluster analysis, or deviation score analysis in combination with regression aim to overcome some of the liabilities of regression in analyzing configurations, each of these approaches faces significant shortcomings for researchers concerned with configurational analysis (e.g., Fiss 2007, 2009). Interaction effects can be used to test asymmetric configurational hypotheses that correspond to notions of necessity and sufficiency in QCA (Clark, Gilligan, and Golder 2006), but their use tends to be limited to two-way or occasionally three-way effects as higher-order interactions are difficult to interpret and are likely to result in multicollinearity.

In response, a newer class of regression-based approaches to the study of causally complex phenomena that has found some favor among political scientists is the partial observability probit approach proposed in Braumoeller (2003) and extended in Gordon and Smith (2004, 2005). In essence, these regression-based approaches allow researchers to statistically test theories proposing multiple causal paths by modeling the underlying causal processes. The probability of occurrence of each causal factor is modeled as a function of a set of explanatory variables, and these probabilities are then multiplied together to get the overall probability that the event of interest will occur. Although these methods can usefully shed light on causal complexity in a variety of contexts, simulations have shown that the convergence, unbiasedness, and efficiency of the estimates that these methods produce is highly contingent both on the structure of the data used and on the accuracy of assumptions about the data generating process (Braumoeller and Kirpichevsky 2005; Gordon and Smith 2004, 2005).

### Contrasting Measures of Fit

Because the search for multicausal explanations is constitutive to the QCA approach, the main goal of the basic crisp-set QCA (csQCA) approach is to identify causes (or combinations of causes) that are common for cases exhibiting a certain outcome and to distinguish these cases from cases with a different outcome (Ragin 1987). Originally, no measurements of fit were included in the csQCA method. However, this changed with the introduction of consistency and coverage by Ragin (2006b, 2008), which presented a move toward expressing the importance of solutions within QCA. Ragin defines consistency as "the degree to which the cases sharing a given combination of conditions . . . agree in displaying the outcome in question," whereas coverage assesses "the degree to which a cause or causal combination 'accounts for' instances of an outcome." (Ragin 2008, 44).

Although these measurements can, to some extent, be used to qualify results of a csQCA analysis, they take on a more central role in fsQCA, as consistency is used to identify a subset of combination that exceed a given consistency threshold before reducing these combinations to identify more parsimonious solutions (Ragin 2008). By including the degree of consistency into the analysis itself, fsQCA introduces a measurement of fit based on set theory into the logic of QCA. Given the plethora of fit measures currently available to the skilled econometrician, it is not possible for us here to provide an extensive comparison between these fit measures and QCA-based fit measures. Instead, we focus on some basic differences in the nature of how fit is conceived in QCA. In particular, it is important to note that fsQCA applies a different criterion to determine "fit" than standard econometric analysis. Whereas, for example, an ordinary least squares (OLS)-based linear regression assumes a linear and thus symmetric relationship between independent and dependent variable, this is not the case in fsQCA, which assumes an asymmetric model of causality; in fsQCA, cases with a high value on a sufficient condition will always display high values of the outcome, but the inverse



**Figure 1.** Relationship between condition and outcome fully consistent with sufficiency but with a low level of correlation in a regression analysis.

is not the case; in fact, cases with a low value on the condition may display both high *and* low values on the outcome. In situations of perfect consistency, all cases will show higher or equal values for the outcome than for the conditions considered. This means that, contrary to a linear regression, a high degree of consistency with sufficiency is present even if many cases show much higher values for the outcome than for the condition in consideration, as shown in Figure 1.

The fact that a data pattern such as the one shown in Figure 1 may be characterized by perfect consistency is a consequence of the multicausal notion of causality found in all varieties of QCA. In a linear regression, these cases would be assumed to contradict the underlying model, resulting in a low measurement of fit. In fsQCA, such cases showing a low value for the condition but a high value for the outcome indicate not so much "misfit" as they indicate an incomplete specification of the causal models; a different condition will have to be identified to account for the outcome in these cases.

Due to its ability to distinguish between necessary and sufficient conditions, fsQCA is able to offer the researcher a comprehensive analysis of the relationship between a causal condition and an outcome in question. In fsQCA, sufficient conditions must be differentiated from necessary conditions; whereas the degree of sufficiency of a condition indicates how far a condition can be related to the explanation of an outcome, the degree of necessity indicates how far a condition is necessary for an outcome to occur. Nonetheless, a data distribution showing a high measurement of fit in a regression analysis, as shown in Figure 2, will also show high levels of sufficiency as well as necessity with consistency in fsQCA. **Figure 2.** Relationship between causal condition and outcome highly consistent with both necessity and sufficiency (>0.9) and a high level of correlation in a linear regression.

Second, fsQCA offers a second measure of fit that assesses the coverage of a causal condition or a causal combination, thus providing an indicator of the scope of a causal condition in accounting for the outcome. This makes coverage comparable in spirit to coefficient of determination  $(R^2)$  that accounts for the proportion of variation in the outcome accounted for by the independent variables. However, it is again important to note that, unlike a correlation-based measure such as an  $R^2$ , coverage is an asymmetric measure. As such, coverage allows the researcher to assess how much of the variation in the outcome is accounted for by a causal condition. However, was the researcher to examine the inverse relationship-how much variation in the causal condition is accounted for by the outcome-a different value would be obtained.

## Integrating Approaches: Opportunities for Complementary Insights

So far, we have focused on contrasting the insights generated using a QCA approach with those using more standard econometric methods. It seems evident that the two approaches are based on rather different philosophies regarding the spirit and nature of social science research; we nevertheless see considerable opportunities for not only using both approaches in a contrasting manner but to draw on both approaches in an integrative manner. This would involve going beyond triangulation involving data analysis based on either approach and comparing the results (e.g., Fiss 2011; Grofman and Schneider 2009), and going toward developing hybrid methods incorporating elements from both approaches. While a full discussion of such methods is beyond the scope of this article, we want to provide an outline of what such integrative methods might look like and what insights they might provide.

From the perspective of the large-*N* QCA researcher, there would appear to be at least two ways in which a regression-based approach might usefully be integrated with a set-theoretic approach.<sup>2</sup> The first one relates to the reintroduction of QCA solutions into a regression framework to test for robustness, establish effect sizes, and address concerns regarding omitted variables in the QCA. The second one takes a slightly different approach by drawing on recent work in lattice theory to mimic a QCA approach within a regression framework to test for complementarity or substitutability between causal conditions. We now address each of these in turn.

## Using QCA Solutions in a Regression Framework

When used in a large-*N* setting, there are in fact several ways in which QCA allows the researcher to either explore or test hypotheses about configurations that are sufficient to bring about the outcome in question, such as examining the sufficiency of a given combination using inferential statistics (e.g., Ragin 2000) or examining whether the consistency of an overall solution obtained by a truth table analysis exceeds a specified threshold. In addition, the researcher has the option of evaluating the necessity of either individual conditions or combinations of conditions. However, one of the strengths of the QCA approach-making explicit that the construction of sets crucially affects the results obtained—is also one of its weaknesses in the sense that it is frequently difficult to obtain stable results. At times, apparently small changes in calibration or the choice of cut-off values regarding frequency and consistency thresholds can precipitate significant changes in the solutions obtained (Skaaning 2011). Although this is in principle no different from the situation faced in a correlational analysis, where transformation of variables, inclusion or exclusion of controls, or the choice of functional form can likewise have significant effects on the results found, it still raises the question of how robustness checks might be constructed to validate the solutions obtained in a QCA.<sup>3</sup>

One possible way to create an integrated approach involves entering the solutions obtained by a QCA into a regression analysis. For instance, assume for simplicity's sake that a fuzzy-set QCA has resulted in solution with two configurations that are sufficient to bring about the outcome:  $A \cdot B \cdot C$  and  $A \cdot B \cdot D$ . The researcher could then calculate the membership of each case in each configuration as the minimum across each of the three conditions involved, that is, min( $A \cdot B \cdot C$ ) and min( $A \cdot B \cdot D$ ),



and save the resulting values as new variables. These new variables, which now stand for the configurations obtained, can then be used in a standard regression analysis to predict the outcome in question. If the correlation between these newly created variables is quite high and multicollinearity is thus a concern, the researcher could also choose to create an additional variable, which is the maximum across the two variables, following an approach commonly used in deviation score analysis that aims to assess overall fit (e.g., Doty et al. 1993). Alternatively, the researcher might create dummy variables coded 1 for cases that have membership scores  $\geq 0.5$  in the configuration and thus present good instances of that corner of the multidimensional property space. The advantage of that approach is that it creates a stronger contrast to cases that have lower membership in both the configuration and the outcome. Either way, a significant advantage of this approach is that the researcher can now estimate regression weights for paths obtained from a QCA and thus calculate the relative importance of each path. Because the outcome variable will normally also be a set and thus have restrictions in its range, a two-limit Tobit regression will usually be more appropriate than OLS regression when the dependent variable is truncated (Long 1997), as is the case with a fuzzy set.

The approach described here also has an additional advantage in that it allows the researcher to introduce further control variables into the analysis—a key challenge for the large-N QCA researcher who is unlikely to have the same familiarity with each case as the small-N QCA researcher, thus raising the issue of whether omitted causal conditions may in fact be driving the findings. Of course, in a traditional QCA, the notion of "controls" is usually not part of the analysis, as QCA does not consider isolating and estimating independent effects of causal variables as the central goal of analysis but instead focuses on combinations of causally relevant conditions (e.g., Ragin 2005). However, this approach comes at a cost, as the inclusion of each additional causal condition exponentially increases the number of configurations that need to be examined, with more than ten conditions making the analysis rather unwieldy. In contrast, incorporating solutions into a regression analysis would allow QCA researchers to examine whether the solutions identified also hold up when other relevant control variables are entered along with these solutions into a regression model.

The advantage of such a hybrid approach seems obvious, and we believe introducing such additional analyses would likely allow insights from large-*N* QCA to become more robust through comparison across methods and more precise in assessing the magnitude of relationships. Of course, there are also tradeoffs, as this kind of hybrid approach moves the analysis much further into the direction of causal homogeneity and additivity—a direction that the QCA approach was designed to avoid. In particular, incorporating paths into a regression analysis means results obtained from an analysis based on set membership are now examined in an analysis based on correlation. For paths that are consistent with a sufficient set relation but low coverage, the regression analysis may be unlikely to show a significant correlation. Accordingly, paths that are qualitatively important but empirically rare may not be picked up by such an analysis, a fact that the researcher would need to take into account in an interpretation of the results as a robustness check. However, when used in addition to rather than as a substitute for the set-theoretic analysis and with an eye toward understanding the inherent differences in emphasis between both methods, these tradeoffs seem acceptable for the pragmatic researcher aiming to get a fuller view of the patterns inherent in the data under analysis.

## An Alternative Approach Based On Lattice Theory

The approach we have discussed so far uses the results from a QCA to create variables for usage in a regression analysis, thus aiming to exploit the ability of a set-theoretic analysis to deal with complex causality and identify configurations that can then be analyzed using analyses based on the general linear model. However, another potential way of integrating QCA with econometrics is based on the mathematics of optimization of functions on lattices (Milgrom and Roberts 1990, 1995; Topkis 1978).<sup>4</sup> Recently, this approach has been used to econometrically test for complementarity or substitutability between elements of a configuration by estimating the effects of configurations of binary explanatory variables on a dependent variable (Cassiman and Veugelers 2006; Mohnen and Röller 2005). Similarly to QCA, a latticetheoretic approach allows for the identification of necessary and sufficient conditions, equifinality, asymmetric causality, and for identifying causally core elements of the configuration. Furthermore, the ability to test for complementarity between elements of the configuration may offer researchers a more fine-grained insight into what drives the association between configurations and outcomes, and may help direct theory-building efforts toward understanding the mechanisms through which such complementarities come about. Finally, this approach can be used to check the robustness of QCA results to the inclusion of numerous control variables that may affect the outcome but could not be included as causal conditions in QCA.<sup>3</sup>

The key feature of the lattice-theoretic approach for our purposes is its definition of complementarity between two activities. Suppose that an actor (such as a firm, a state, and a political party) engages in two activities, A and B, either or both of which it can choose to perform. Accordingly, there are then four possible configurations of activities that the actor may end up choosing:

Configuration 1: neither A nor B ( $\sim A \bullet \sim B$ ) Configuration 2: not A but B ( $\sim A \bullet B$ ) Configuration 3: A, but not B ( $A \bullet \sim B$ ) Configuration 4: both A and B ( $A \bullet B$ )

A and B are complementary in an outcome function V(.) if  $V(A \bullet B) - V(\sim A \bullet B) > V(A \bullet \sim B) - V(\sim A \bullet \sim B)$ . To restate, A and B are complementary if the return to performing activity A is greater if activity B is already being performed than if it is not. The above definition of complementarity also applies to set-theoretic logic if we take the consistency of solution membership in an outcome set Y as the outcome function V(.). Suppose that the configuration A•B is always a subset of the outcome of interest so its consistency is 100 percent, whereas the remaining three configurations are never subsets of the outcome with consistencies of 0 percent. Substituting these consistency values into the definition of complementarity given above we get: 100% (V(A•B))- 0%  $(V(\sim A \bullet B)) > 0\% (V(A \bullet \sim B)) - 0\% (V(\sim A \bullet \sim B))$ . In this case, A and B are clearly complementary, but this is not particularly interesting as both A and B are necessary but insufficient conditions that must both be met to create the outcome.

To see that knowing more about complementarity (or substitutability) relationships than QCA results can uncover might be worthwhile, let us slightly alter the above example by giving the solution A•~B a consistency score of .80. Substitution gives: 100% (V(A•B)) – 0% (V(~A•B)) > 80% (V(A•~B)) – 0% (V(~A•~B)). Again, A and B are clearly complementary, but this case is more interesting than the first one because QCA (assuming a consistency cut-off  $\leq$  .80 and no remainders) would produce a parsimonious solution A  $\rightarrow$  *Y*, suggesting that B has no influence on the outcome. However, this is not the case as the choice of B when A has already been chosen has the rather substantial effect of increasing the consistency of the solution from 80 to 100 percent.

The lattice-theoretic approach has been used as the basis for econometric tests for complementarity in the field of innovation in the following manner (Mohnen and Röller 2005): First, a researcher runs the following regression analysis:

$$V = \beta_1(\sim A \bullet \sim B) + \beta_2(\sim A \bullet B) + \beta_3(A \bullet \sim B) + \beta_4(A \bullet B) + \gamma^2 \mathbf{Z} + \varepsilon,$$

where V is the dependent variable, (~A•~B) and other possible configurations are binary dummy variables taking the value of 1 for observations in which these configurations are observed and 0 otherwise,  $\beta_n$  (n = 1,2,3,4) are the estimates of the effect of these configurations on the dependent variable, conditional on a vector the control variables  $\mathbf{Z}$ , and  $\varepsilon$  is an error term.<sup>6</sup> The dependent variable can be continuous, binary, or categorical.

Like QCA, this specification allows for the identification of necessary and sufficient conditions, equifinality, asymmetric causality, and for identifying causally core conditions. If  $\beta_3$  is not significantly different from  $\beta_4$ , and if both of these coefficients are larger than  $\beta_1$  and  $\beta_2$  $(\beta_3 \approx \beta_4 > \beta_1, \beta_2)$ , then this is evidence that A is both a necessary and a sufficient condition for maximizing the probability of V occurring, conditional on the control variables **Z**.<sup>7</sup> Both A and B would appear to be necessary but insufficient conditions for V if  $\beta_4 > \beta_1, \beta_2, \beta_3$ . Finally, if  $\beta_2 \approx \beta_3 \approx \beta_4 > \beta_1$ , this suggests that both A and B are sufficient but unnecessary conditions for V.

The results suggest equifinality if the difference between the largest and second-largest betas is not statistically significant.<sup>8</sup> If  $\beta_2 \approx \beta_3 > \beta_1, \beta_4$ , this is evidence of asymmetric causality as the absence of a configuration associated with V (e.g., A•~B) will not necessarily lead to the absence of V. This is because (~A•B) is also associated with V. Furthermore, if  $\beta_3 \approx \beta_4 > \beta_1, \beta_2$ , then A can be inferred to be a causally core condition, whereas B does not appear to affect the outcome (the QCA equivalent of this result would be a complex solution A•B + A•~B → V, which simplifies to a parsimonious solution A → V).

The number of control variables to be included is the analysis limited solely by the degrees of freedom available in the data set, unlike QCA, where the number of causal conditions to be assessed faces greater constraints and "controlling" is usually not a goal of the analysis. If the estimated betas in the above regression are statistically significant and are not all equal to each other, a test for complementarity between conditions A and B can be performed.

To test for complementarity, substitute the estimated betas from the above regression into the lattice-theoretic definition of complementarity: A and B are complementary if  $\beta_4 - \beta_2 > \beta_3 - \beta_1$ . The statistic used to test whether this condition holds or not is a Wald distance test statistic, which corresponds to the minimum distance between the vector of estimated betas and a vector of hypothetical betas, which conforms to the definition of complementarity. In practice this statistic is calculated by using the estimated betas and their variance-covariance matrix to solve a minimization problem with inequality constraints.9 Upper and lower bound critical values, which can be used to interpret this test statistic are given in Kodde and Palm (1986). In addition to testing the null hypothesis of complementarity, the null hypothesis of substitutability should also be tested. Doing so allows the researcher to see whether his data have the power to distinguish between the two hypotheses. This approach to testing for complementarity has been extended to test for pairwise complementarity in a set of more than two configurational elements (Mohnen and Röller 2005), and can easily be extended further to test for complementarity between combinations of numerous configurational elements.

A limitation of the lattice-theoretic approach described above is that configurational elements must be in binary form—either being used or not, with no allowance for degrees of implementation, unlike fuzzy sets. A further significant limitation is that the approach requires observations on all possible configurations for complementarity testing to be possible. If the researcher is interested in numerous causal conditions relating to social phenomena, it is highly unlikely that a given data set will have observations on all possible configurations of these conditions. This commonly occurring lack of observations on some configurations of causal conditions, known as limited diversity to practitioners of QCA, presents perhaps the main opportunity and the main challenge for integration of QCA with the lattice-theoretic approach.

The potential for integration arises from QCA being equipped to deal with limited diversity through the use of easy and difficult counterfactuals (Ragin 2008), thereby allowing for the differentiation between causally core, causally peripheral, and irrelevant conditions (Fiss 2011). When not all logically possible configurations are observed in the data, preventing the researcher from using a lattice-theoretic approach, QCA counterfactual analysis could be used to identify conditions that appear to be causally core. If not all conditions are found to be causally core, the number of possible configurations of causally core conditions be analyzed using the latticetheoretic approach will be significantly lower than the number of configurations used in the QCA, and these configurations will be less likely to exhibit limited diversity. The lattice-theoretic approach could then be applied to test for complementarity between causally core conditions only, with noncore causal conditions being added to the set of control variables. QCA thus makes lattice-theoretic complementarity testing possible, and researchers using QCA may also benefit from following their analysis with a lattice-theoretic test of complementarity between core causal conditions to get insights about the relationship between the causal conditions and the outcome that could not be seen in the QCA results. In addition, the lattice-theoretic approach can also serve as a means of checking the robustness of QCA results to the inclusion of a large set of control variables and to the use of a continuous dependent variable.

A limitation of this combined approach is that there is of course no guarantee that the narrowing down of the set of causal conditions to include only those identified as being causally core by QCA will result in data that do not exhibit limited diversity. In such cases, the lattice-theoretic approach may still serve a purpose as a robustness check, but it would not be possible to carry out the complementarity-testing procedure. Finally, this approach to integrating QCA and regression depends upon the QCA counterfactual analysis procedure to narrow down the set of causal conditions. Future work developing the hybrid QCA-lattice-theory approach should therefore investigate the extent to which the omission of control variables, which are to be used in the lattice-theoretic analysis, from the set of causal conditions included in the QCA stage may produce QCA results that fail to identify core causal conditions that affect the outcome in a configurational manner with one or more of the omitted variables.

## Conclusion

As QCA researchers broaden their scope of inquiry to not only include small-N situations but also large-N situations, the changes in associated terrain and competition from established econometric approaches necessitate new ways to conceptualize set-theoretic inquiry. The goal of our article has been to facilitate this development and to provide some direction regarding this extension of the QCA approach as well as drawing out promising opportunities to engage and integrate with econometric methods. To the QCA purist, this might appear to be problematic, given the deep-running philosophical differences between the settheoretic and correlation-based approach; QCA is focused on the way that causal conditions combine, whereas regression analysis focuses on isolating net-effects. We do not wish to downplay these differences, and believe that our prior discussion has aimed to further clarify the relationship between QCA and correlation-based methods as both converge in their focus on large-N phenomena. Indeed, we believe that our argument for exploring the further integration of QCA and econometrics will only succeed if researchers are well aware and appreciative of these differences, as they are the basis for understanding the opportunities for complementarities between both approaches. Nevertheless, we feel that a push toward further potential integration and hybrid research strategies is in fact well founded on the pragmatic philosophy that underlies QCA and is reflected in its philosophy of engaging in a dialogue with the data. In our view, this integration presents an important and promising area of work that will require considerable methodological advancement. Much work remains, but we believe there is also much to be gained as we explore opportunities for added insight drawing on the strengths of each approach.

#### Notes

- Although Vis (2012) refers to fifty to hundred cases as "moderately large N," we believe that settings with roughly hundred cases or more are commonly considered fully in (or almost fully in) the set of "large-N" studies.
- A number of integrative approaches that we do not discuss have been proposed. One particular integrative approach that appears to hold some promise is the use of QCA to create a meaningful typology of entities at one level of analysis

before using dummy variables created according to this typology to account for contextual effects in a regression performed at lower level of analysis. Dotti Sani and Quaranta (2011) use such an approach to study the work-motherhood relation in Organisation for Economic Co-operation and Development (OECD) countries. Focusing on formally accounting for measurement error, Eliason and Stryker (2009), in another approach, do use goodness-of-fit tests to qualify the fit of fuzzy-set conditions and thereby to adapt fsQCA results to inferential logic based on falsification.

- 3. Maggetti and Levi-Faur (this issue) discuss strategies for dealing with potential measurement error in QCA, whereas Emmenegger, Kvist, and Skaaning (this issue) review comparative welfare-state research using QCA and find that not all studies carried out robustness checks of their findings.
- 4. Although the interested reader is encouraged to read these articles for a formal treatment of optimization on lattices and for the relevant mathematical proofs, we shall focus our discussion of this approach on the results necessary for its econometric operationalization.
- Dealing with Errors in QCA

- 5. The potential connection of lattice theory with (fs)QCA is also suggested by Zaytsev et al. (2012), who combine QCA with formal concept analysis (FCA) based on lattice theory to address problems of measurement in democracy studies.
- The regression produces estimates for all four betas as it does not include a constant.
- 7. If V is continuous, then this result suggests that A is a necessary and sufficient condition for high V. If  $\beta_3 \approx \beta_4 < \beta_1, \beta_2$  then this would suggest that A is a necessary and sufficient condition for low V.
- 8. If V is continuous, the above result would suggest equifinality with respect to a high V outcome. More generally for a continuous V, if the difference between two or more estimated betas is not statistically significant, these configurations are equifinal as they are mutually exclusive yet associated with the same value of the outcome variable.
- See Mohnen and Röller (2005) for details of the test statistic and of the inequality-constrained minimization problem used to calculate it.

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#### Abstract

This paper discusses five strategies to deal with five types of errors in Qualitative Comparative Analysis (QCA): condition errors, systematic errors, random errors, calibration errors, and deviant case errors. These strategies are the comparative inspection of complex, intermediary, and parsimonious solutions; the use of an adjustment factor, the use of probabilistic criteria, the test of the robustness of calibration parameters, and the use of a frequency threshold for observed combinations of conditions. The strategies are systematically reviewed, assessed, and evaluated as regards their applicability, advantages, limitations, and complementarities.

## Introduction: Errors and Criticisms of QCA

Strategies to deal with the possibility of error are essential tools in all types of social research. The challenge of error management can be broadly conceived as the challenge of forming a bridge between theory and empirical research in a world where some imprecision, uncertainty, and randomness is unavoidable. Any research study in the social sciences must contend with error, stemming from a variety of sources, including incomplete definitions of the constructs being measured, imperfect operationalization of the ideas contained in the corresponding concepts, and weaknesses of methods of assessment. This holds of course also for QCA, that, some argue, has limited capacity to deal with different types of errors that are commonplace in the social sciences. As QCA methods typically work under deterministic or quasi-deterministic assumptions, standard statistical techniques that are used to correct and minimize measurement error and other types of error do not apply. The researcher cannot straightforwardly

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methods. The topic of set-theoretic MMR involves more issues than we have discussed here. There are important differences between process tracing after a QCA of necessity, vs. a QCA of sufficiency. For example, sufficient solutions usually involve conjunctions and, in contrast to necessity, cases that reduce coverage are targets for process tracing (Schneider & Rohlfing forthcoming). Further exploration of these differences is a worthwhile endeavor to strengthen causal inferences in research on necessity and sufficiency alike.

### Notes

- See Eliason and Stryker (2009) for a different procedure for the analysis of necessary conditions. Dion (1998) uses a Bayesian approach for the analysis of necessary conditions.
- Rihoux and Lobe's (2009) terms "upstream" and "downstream"—introduced in their discussion of the Qualitative Comparative Analysis (QCA) research process and the role of case knowledge therein—only partially overlap with ours.
- 3. We say "main purpose" because, even in post-QCA process tracing, one might find hitherto overlooked evidence for changes in the population, concepts, measurement, and calibration.
- 4. We use this example for illustrative purposes only.
- 5. As mentioned, *MA* alone is not necessary. We nevertheless start with a single condition to illustrate process tracing in the most basic setting of just one condition to identify potentially omitted terms.
- Using simulated data, an online appendix to our paper demonstrates that our formulas produce plausible results (http://prq.sagepub.com/supplemental/).
- 7. If the formula nevertheless yields the same score for multiple cases, one should choose the one with higher membership in *Y*.
- This holds true because the logical OR operator requires assigning cases the *maximum* set membership across all conditions combined by logical OR (Ragin 2000, 175).
- 9. Alternatively, they contribute to the trivialness of the necessary condition (Goertz 2006; Ragin 2006; Schneider and Wagemann 2012).
- 10. Pre-QCA studies of cases in Zone 3 might help to identify measurement and/or calibration error in either *X* (membership too easy) or *Y* (membership too difficult) and increase the relevance of *X*. These are not model-related modifications as we define them, though.
- 11. Goertz (2008, 11) calls this "choosing cases diversely."
- 12. Typical cases that are joint members should only be chosen if no unique members are available.
- This selection strategy is the set-theoretic equivalent to the diverse case strategy (Seawright and Gerring 2008; Rohlfing 2012, chap. 3).
- 14. If two or more pairs of cases obtain the same score, researchers should choose the one with the largest difference in *Y*.

- 15. We know that the entire truth table row to which the typical case belongs is sufficient for the outcome. Every condition constituting this row is an INUS condition, and taking away any of these conditions might lead to the absence of the outcome (assuming that we analyze unique members and that the condition is not logically redundant). Consequently, case selection for comparative process tracing in the typical case and the IIR case must ensure that all INUS conditions are present in these cases.
- 16. Note that for process tracing on the mechanism behind the pattern of necessity, it only matters that cases are members of similar truth table rows, not how strong their membership in these rows are.
- 17. If two or more pairs of cases obtain the same score, researchers should choose the one with the largest difference in *Y*.
- See the truth table in the online appendix (http://prq.sagepub.com/supplemental/).
- If two or more pairs of cases obtain the same score, researchers should choose the one with the largest sum of membership scores in Y.
- In the ideal scenario, the deviant cases consistency turn into typical cases if we were to add the omitted term to the solution.
- 21. If two or more pairs of cases obtain the same score, researchers should choose the one with the largest difference in *Y*.

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